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## Exercise 1

Friday, October 20, 2017

Problem 1. (Matrix Vector Multiplication by Map-Reduce)
Let $\mathbf{A} \in \mathbb{R}^{n \times m}$ be a matrix with large dimensions $n$ and $m$.
a) Let $\mathbf{v} \in \mathbb{R}^{m}$ be a vector. Explain a way to execute the multiplication of $\mathbf{A}$ and $\mathbf{v}$ using MapReduce.
b) Let $\mathbf{B} \in \mathbb{R}^{m \times k}$ be a matrix. Explain a way to execute the multiplication of $\mathbf{A}$ and $\mathbf{B}$ using MapReduce.

Problem 2. (Sparse Vectors with Map-Reduce)
Let $\mathbf{v} \in \mathbb{R}^{n}$ be a sparse vector with large dimension $n$.
a) Let $\mathbf{w} \in \mathbb{R}^{n}$ be a sparse vector. Explain a way to execute the sum of $\mathbf{v}$ and $\mathbf{w}$ using MapReduce.
b) Explain a way to execute the average squared value $\frac{1}{n} \sum_{i=1}^{n}\left(v_{i}\right)^{2}$ using MapReduce.

